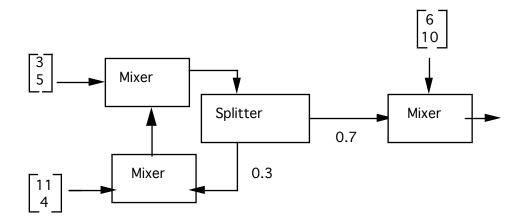
- 1. Construct the L/U algorithm using the Crout decomposition, using the same notation as in class.
- 2. For the following system of linear equations
 - a) Solve using Gauss elimination
 - b) Develop the LU factors and calculate the determinant
 - c) Resolve using L and U for the RHS provided

$$2x_1 + 4x_2 - x_4 = b_1$$
$$-x_3 + x_4 = b_2$$
$$x_1 + 6x_2 + 7x_3 = b_3$$
$$x_1 + x_4 = b_4$$
$$\underline{b}^T = (3,2,5,4)$$

- 3. Retrieve the LU and QR decomposition programs from LINPACK in NETLIB and solve problem 2 again using both procedures. Alternately, MathCAD or MATLAB may be used.
- 4. Derive the linear balance equations for the problem



- a) Develop pivot sequences using the Markowitz criterion. Indicate the number of new non-zero elements created in developing L and U.
- b) For this case calculate L and U and solve the material balance equations.

1) Let r=1
2) let urr=1
3) Denerate column r for L

lir = air - 2 lik ukr it >r

4) Denerate row r for U

Urj = (arj - 2 lrk ukj)/lrr jor

Urj = (arj - 2 lrk ukj)/lrr jor

5-) Solve Ly=5 yi=(bi-2lij yj)/kii=1, n

Ux=y zi=(yi-2,uijzj) i=1, n

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2 a) Janvian elimination $2x_1 + 4x_2 - x_4 = 3$ $x_1 + 6x_2 + 7x_3 = 5$ -73 + 24 = 22 + 24 = 4 $\begin{bmatrix} 2 & 4 & 0 & -1 & 3 \\ 1 & 6 & 7 & 0 & 5 \\ 0 & 0 & -1 & 1 & 2 \\ 1 & 0 & 0 & 1 & 4 \end{bmatrix} \begin{bmatrix} 2 & 4 & 0 & -1 & 3 \\ 0 & 4 & 7 & 1/2 & 7/2 \\ 0 & 0 & -1 & 1 & 2 \\ 0 & -2 & 0 & 3/2 & 5/2 \end{bmatrix}$ 0 4 7 1/2 7/2 0 0 -1 1 2 0 0 7/2 7/4 17/4 $\gamma_2 = 0.3571$ x3 = 0.1428 $x_4 = 2.1429$ b) L/V decomposition

$$\det(A) = \det(L) \det(U) \begin{vmatrix} 2 & 4 & 0 & -1 \\ 0 & 4 & 7 & 1/2 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 0 & 2^{1/4} \end{vmatrix}$$

$$= (-42)(-1)$$
one row exchange = 42

c) alternate right hand side;

$$U_{\chi} = y$$
 $\chi = \begin{bmatrix} -2.667 \\ 3.0 \\ -1.333 \\ 5.667 \end{bmatrix}$

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$$\begin{bmatrix} -1 & 1 & 0 & 0 & 2 \\ 0 & 1 & 1 & 0 & 4 \\ 0 & -1 & 2 & 4 & 3 \\ 0 & 7 & 1 & 6 & 19 \end{bmatrix} \begin{bmatrix} -1 & 1 & 0 & 0 & 2 \\ 0 & 1 & 1 & 0 & 4 \\ 0 & 0 & 3 & 4 & 7 \\ 0 & 0 & -6 & 6 & -9 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 1 & 0 & 0 & 2 \\ 0 & 1 & 1 & 0 & 4 \\ 0 & 0 & 3 & 4 & 7 \\ 0 & 0 & 0 & 14 & 5 \end{bmatrix} \qquad \begin{array}{c} \chi_1 = 1.8571 \\ \chi_2 = 0.3571 \\ \chi_3 = 0.14286 \\ \chi_4 = 2.14286 \end{array}$$

3. Verify solutions for #2 with QR + LU.



Markowitz

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can yield some requence et min row/
min coll for this problem nonsenique b) solution to many baldness problem. $M_{12} = \begin{bmatrix} 17 \\ 7.86 \end{bmatrix}$ $M_{13} = \begin{bmatrix} 6 \\ 3.86 \end{bmatrix}$ $M_{23} = \begin{bmatrix} 20 \\ 12.86 \end{bmatrix}$ $M_{34} = \begin{bmatrix} 14.0 \\ 9 \end{bmatrix}$ $\mathcal{M}_{45} = \begin{bmatrix} 20 \\ 19 \end{bmatrix}$

and the contract the first of particles are seen to be supplied that the second of the